

Relative Frequency

KS3 Maths · Follows the national curriculum

Name _____ Class _____ Date _____

1. Worked example

A coin is flipped 50 times and lands on heads 23 times. Find the relative frequency of heads.

Step 1 · Relative frequency = frequency $\div$ trials

$$23 \div 50$$

Step 2 · Calculate

$$0.46$$

Answer: 0.46 (or 23/50)

Check: Close to the theoretical 0.5, for a fair coin with 50 flips ✓

2. Now try one with the steps

A fair dice is rolled 300 times. How many 6s would you expect?

Step 1 · P(6) for a fair dice

Step 2 · Expected number = probability $\times$ trials

Answer:

3. Practice

Show your working. The marks tell you how much is expected.

1. A coin is flipped 40 times and lands on heads 18 times. Find the relative frequency of heads. [1]

2. A fair dice is rolled 600 times. How many times would you expect to roll a 4? [1]

3. The probability it rains on any day in April is 0.3. How many rainy days would you expect in the 30 days of April? [1]

4. A spinner lands on red 70 times in 200 spins. Find the relative frequency of red. [1]

5. Counters are taken from a bag and put back 50 times. A green counter is taken 12 times. Estimate $P(\text{green})$. [1]
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6. Which gives a more reliable estimate of a probability: 20 trials or 500 trials? [1]
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7. Zane scores 18 penalties out of 24. What is the relative frequency of him scoring? [1]
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8. Using the spinner that landed on red 70 times in 200 spins, estimate how many reds there would be in 1000 spins. [2]
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9. A drawing pin lands point up 64 times in 160 throws. Find the relative frequency of point up. [1]
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10. Using the drawing pin results, how many times would you expect it to land point up in 1000 throws? [2]
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11. The relative frequencies of outcomes A and B are 0.2 and 0.35. A, B and C are the only outcomes. What is the relative frequency of C? [1]
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12. A dice is rolled 120 times. How many 6s would you expect if it is fair? [1]
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13. That dice actually showed a 6 on 38 of the 120 rolls. What does this suggest? [2]
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14. Using Zane's record of 18 goals from 24 penalties, how many goals would you expect from his next 40 penalties? [2]
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15. A bag holds 10 counters. A counter is taken and replaced 100 times, and 31 are red. Estimate how many of the 10 counters are red. [2]
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4. Before you hand it in

Flipping a fair coin 10 times, getting 6 heads, and saying the coin is biased

Random results vary. With 10 flips, 6 heads is very normal. Only a big difference over MANY trials suggests bias.

'It has landed on tails five times in a row, so heads is due next'

A coin has no memory. P(heads) on the next flip is still 1/2, whatever happened before.

Relative frequency of heads = $23 \div 27$ (heads $\div$ tails)

Divide by the TOTAL number of trials: 23 heads in 50 flips gives $23 \div 50 = 0.46$.

Expected number of 6s in 50 rolls = 8.333..., so you will get 8

The expected number is an average over many repeats. You might get 5 or 12 sixes. Say 'about 8'.