

3d Shapes

KS3 Maths · Follows the national curriculum

Name _____ Class _____ Date _____

1. Worked example

Find the surface area of a cuboid 4cm × 3cm × 2cm.

Step 1 · Find the area of each pair of faces

Top/bottom: $4 \times 3 = 12$. Front/back: $4 \times 2 = 8$. Sides: $3 \times 2 = 6$

Step 2 · Apply the formula

$$SA = 2(12 + 8 + 6) = 2 \times 26$$

Step 3 · Calculate

$$= 52\text{cm}^2$$

Answer: 52cm^2

Check: 6 faces total: $2 \times 12 + 2 \times 8 + 2 \times 6 = 24 + 16 + 12 = 52$ ✓

2. Now try one with the steps

Find the volume of a triangular prism 12 cm long whose triangular end has base 8 cm and height 5 cm.

Step 1 · Area of the cross-section (the triangle)

Step 2 · Volume = cross-section area × length

Answer:

3. Practice

Show your working. The marks tell you how much is expected.

1. Find the volume of a cuboid measuring 5cm × 4cm × 3cm. [2]

2. Find the volume of a cube with side length 6cm. [2]

3. Find the volume of a cylinder with radius 4cm and height 10cm. (Use $\pi = 3.14$) [3]

4. Find the surface area of a cube with side length 5cm. [2]

5. A triangular prism has a triangular cross-section with area 12cm^2 and length 8cm. Find its volume. [3]

6. A cuboid has volume 120cm^3 . Its length is 6cm and width is 5cm. Find its height. [3]

7. Find the volume of a cuboid measuring $10\text{ cm} \times 2\text{ cm} \times 3\text{ cm}$. [1]

8. How many faces, edges and vertices does a cuboid have? [2]

9. How many 1 cm cubes fit exactly into a box measuring $5\text{ cm} \times 4\text{ cm} \times 3\text{ cm}$? [1]

10. A cube has a volume of 64 cm^3 . How long is each edge? [1]

11. A triangular prism is 10 cm long. Its triangular end has base 6 cm and height 4 cm. Find its volume. [2]

12. A prism has a cross-section of area 18 cm^2 and a volume of 270 cm^3 . How long is it? [2]

13. Find the surface area of a cuboid measuring $6\text{ cm} \times 4\text{ cm} \times 2\text{ cm}$. [3]

14. Find the volume of a cylinder with radius 3 cm and height 5 cm. Use the π button and give your answer to 1 decimal place. [2]

15. A fish tank measures 50 cm $\times$ 30 cm $\times$ 40 cm. How many litres of water does it hold when full? (1 litre = 1,000 cm³) [3]

16. A cylinder has a volume of 500 cm³ and a radius of 5 cm. Find its height to 1 decimal place. [3]

4. Before you hand it in

Using a 2D area formula (like length $\times$ width) for volume of a 3D shape

Volume always involves THREE dimensions multiplied together (or area $\times$ length for prisms). Area is for flat 2D shapes only — volume needs an extra dimension.

Forgetting to multiply the cross-sectional area by the length for a prism

For prisms: Volume = (area of the 2D cross-section) $\times$ (length). Find the cross-section area FIRST using the appropriate 2D formula, THEN multiply by length.

Thinking 1 m³ = 100 cm³

1 m = 100 cm, so 1 m³ = 100 cm $\times$ 100 cm $\times$ 100 cm = 1,000,000 cm³. For areas, 1 m² = 10,000 cm².