

Simultaneous Equations

GCSE Maths · Written to the shared content for AQA, Edexcel and OCR

Name _____ Class _____ Date _____

1. Worked example

Solve $x + y = 8$ and $2x - y = 7$.

Step 1 · $+y$ and $-y$: opposite signs, so add

$$3x = 15 \rightarrow x = 5$$

Step 2 · Substitute into $x + y = 8$

$$5 + y = 8 \rightarrow y = 3$$

Answer: $x = 5, y = 3$

Check: $5 + 3 = 8$ ✓ and $10 - 3 = 7$ ✓

2. Now try one with the steps

Solve $3x + 2y = 19$ and $5x + 4y = 33$.

Step 1 · Double the first equation to match $4y$

Step 2 · Same signs: subtract the second equation

Step 3 · Substitute

Answer:

3. Practice

Show your working. The marks tell you how much is expected.

1. Solve $x + y = 10$ and $x - y = 4$. [3]

2. Solve $2x + y = 11$ and $x + y = 7$. [3]

3. Solve $3x + 2y = 16$ and $x - 2y = 0$. [3]

4. Solve $y = 2x$ and $x + y = 9$. [3]

5. Solve $4x + y = 14$ and $2x + y = 8$. [3]

6. Solve $2x + 3y = 12$ and $5x + 3y = 21$. [3]

7. Solve $4x - 3y = 1$ and $2x + y = 13$. [4]

8. Solve $3x + 4y = 10$ and $2x + 3y = 7$. [4]

9. Solve $5x - 2y = 4$ and $3x + 5y = 21$. [4]

10. The lines $y = x + 1$ and $y = 7 - 2x$ are drawn on a grid. Where do they cross? [2]

11. Two numbers add up to 23 and have a difference of 7. Find them. [3]

12. 3 pens and 2 pencils cost £1.90. 1 pen and 4 pencils cost £1.30. Find the cost of a pen, in pence. [4]

13. 2 adult and 3 child cinema tickets cost £38. 1 adult and 2 child tickets cost £22. Find the price of an adult ticket, in £. [4]

14. Explain why $x + 2y = 5$ and $2x + 4y = 8$ have no solution. [2]

15. The line $y = mx + c$ passes through (1, 4) and (3, 10). Use simultaneous equations to find m and c . [3]

4. Before you hand it in

Adding $2x + y = 11$ and $x + y = 7$ to 'eliminate' y

Both y terms are +y (same signs), so SUBTRACT: $x = 4$. Add only when the signs are opposite.

Multiplying only the x term when scaling an equation: $3x + 2y = 19 \rightarrow 6x + 2y = 38$

Multiply EVERY term, including the right-hand side: $6x + 4y = 38$.

Stopping at $x = 5$

Substitute back to find y, and give both values.

Subtracting $-3y$ from $12y$ as $9y$

$12y - (-3y) = 15y$. If the signs are opposite, adding is safer.